

## HW. # 14

Homework problems are taken from several textbooks. The problems are color coded to indicate level of difficulty. The color **green** indicates an elementary problem, which you should be able to solve effortlessly. **Yellow** means that the problem is somewhat harder. **Red** indicates that the problem is hard. You should attempt the hard problems especially.

Sketch the region B and identify it as x-simple, y-simple, both, or neither.

1.  $B = \{(x, y); 0 \leq y \leq x, 0 \leq x \leq 4\}$

2.  $B = \{(x, y); -3 \leq y \leq x^3 - x, -1 \leq x \leq 1\}$

3.  $B = \{(x, y); y^2 \leq x \leq \frac{3y^2}{4} + 1\}$

4.  $B = \{(x, y); e^y \leq x \leq e, 0 \leq y \leq 1\}$

5. B is the bounded portion of the intersection of  $A = \{(x, y); -1 - x^2 \leq y \leq 1 + x^2\}$  and  $C = \{(x, y); -1 - \frac{y^2}{25} \leq x \leq 1 + \frac{y^2}{25}\}$

Evaluate the iterated integral and sketch the region of integration.

6.  $\int_{-2}^0 \int_2^4 (3x^2 + 2y^3) dy dx$

7.  $\int_0^\pi \int_x^\pi y \sin(x) dy dx$

8.  $\int_0^1 \int_{e^{-x}}^{e^x} \frac{\ln(y)}{y} dy dx$

9.  $\int_{-1/4}^1 \int_{-y}^{1-y^2} (5x - y) dx dy$

10.  $\int_0^{\pi/8} \int_0^y \sec^2(x + y) dx dy$

Find the double integral of the function over the indicated region.

11.  $f(x, y) = (x - 2y)^2$ , B is the rectangle with sides parallel to the axes and opposite corners  $(-1, -1)$  and  $(5, 2)$ .

12.  $f(x, y) = \frac{x}{(y+1)^2}$ , B is the region bounded by the parabola  $y = x^2$  and the line  $y = 4x$ .

13.  $f(x, y) = ye^x$ , B is the region bounded by the parabola  $x = y^2$  and the line  $x = 5y$ .

14.  $f(x, y) = x \cos(y) \sin(y)$ , B is the region bounded by the lines  $x = 1$ ,  $x = -1$ , the x-axis, and  $y = \tan^{-1}(x)$ .

Evaluate the double integral over the indicated region.

15.  $\iint_B e^x$ , where B is the rectangle with vertices  $(0, 0)$ ,  $(\ln 2, 0)$ ,  $(\ln 2, 1)$ , and  $(0, 1)$ .

16.  $\iint_B (\cos(x) - y)$ , where B is bounded by  $y = \sin(x)$ ,  $y = 0$ ,  $x = 0$ , and  $x = \pi$ .

17.  $\iint_B x$ , where B is the region in the first quadrant bounded by  $y = 0$ ,  $y = 2$ ,  $x = 0$ , and  $x = 1 + y^2$ .

Find the volume of the indicated solid region.

18. The solid bounded above by the paraboloid  $z = x^2/4 + y^2/9 + 1$ , below by the xy-plane, and lying above the square  $S = \{(x, y); 0 \leq x \leq 1, 0 \leq y \leq 1\}$ .

19. The solid bounded above by the triangle in the xy-plane with vertices  $(0, 0, 0)$ ,  $(2, 0, 0)$ , and  $(1, 1, 0)$ , and bounded below by the plane  $z = -8 + x + y/2$ .

20. The solid bounded by the surface  $z = (1 - x^2)(1 - y^2)$  and the xy-plane.

21. The solid bounded by the paraboloid  $z = x^2 + y^2$  and the plane  $z = 1$ .

Use double integrals to find the area of each of the indicated regions.

22. The quadrilateral with vertices  $(0, 0)$ ,  $(4, 0)$ ,  $(3, 1)$ ,  $(0, 2)$ .

23. A disc of radius 10.

24. The region bounded by the curves  $y = x^3$  and  $x = y^3$ .

Reverse the order of integration.

25.  $\int_0^2 \int_x^2 f(x, y) dy dx$

26.  $\int_0^1 \int_1^{e^y} f(x, y) dx dy$

27.  $\int_{\pi/2}^{\pi} \int_0^{\sin x} f(x, y) dy dx$

28.  $\int_{-4}^4 \int_{-\sqrt{16-y^2}}^{\sqrt{16-y^2}} f(x, y) dx dy$

29.  $\int_{-1}^0 \int_{-x}^1 f(x, y) dy dx + \int_0^1 \int_{\sqrt{x}}^1 f(x, y) dy dx$

30.  $\int_{-1}^1 \int_{y-3}^{y^2} f(x, y) dx dy$